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	Quentin Galand – 0000-0001-5922-8585 Stéfan Van Vaerenbergh – 0000-0002-6614-0458
	Werner Köhler – Oleg Khlybov –
	Tatyana Lyubimova – Aliaksandr Mialdun – 0000-0002-7787-2865
	Valentina Shevtsova – 0000-0001-6109-5048 Thomas Triller – 0000-0002-7763-7865
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### ARTICLE

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# Results of the DCMIX1 experiment on measurement of Soret coefficients in ternary mixtures of hydrocarbons under microgravity conditions on the ISS

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Quentin Galand,<sup>1,a)</sup> <sup>(D)</sup> Stéfan Van Vaerenbergh,<sup>1</sup> <sup>(D)</sup> Werner Köhler,<sup>2</sup> Oleg Khlybov,<sup>3</sup> Tatyana Lyubimova,<sup>3</sup> Aliaksandr Mialdun,<sup>1</sup> <sup>(D)</sup> Ilya Ryzhkov,<sup>4,5</sup> Valentina Shevtsova,<sup>1</sup> <sup>(D)</sup> and Thomas Triller<sup>2</sup> <sup>(D)</sup>

### 9 -

- 10 AFFILIATIONS
- <sup>11</sup> MRC, Université libre de Bruxelles, Department of Chemical Physics, Avenue F. D. Roosevelt, CP165/32, B-1050 Brussels, Belgium
- <sup>12</sup> <sup>2</sup>Physikalisches Institut, Universität Bayreuth, 95440 Bayreuth, Germany
- <sup>13</sup> Institute of Continuous Media Mechanics UB RAS, Koroleva, 1, 614013 Perm, Russia
- 14 <sup>4</sup>Institute of Computational Modelling SB RAS, 660036 Krasnoyarsk, Russia
- <sup>15</sup> <sup>5</sup>Siberian Federal University, Svobodny 79, 660041 Krasnoyarsk, Russia
- <sup>16</sup> <sup>a)</sup>E-mail: ggaland@ulb.ac.be. Tel.: (+32)26506576. Fax: (+32)26503126.

# 18 ABSTRACT

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- <sup>19</sup> The Soret coefficients of a set of ternary systems of 1,2,3,4-tetrahydronaphthalene (THN), isobutylbenzene (IBB), and n-dodecane (nC<sub>12</sub>) at
- 20 298.15 K were measured under microgravity condition aboard the International Space Station in the frame of the DCMIX1 experiment. The
- 21 present work includes a comprehensive study of possible data processing sequences for the interpretation of interferometric Soret experiments
- <sup>22</sup> in ternary systems. Several data processing methodologies are discussed. A significant concentration dependence of the Soret coefficients is
- observed. In the present study, we have obtained large and positive values for THN and negative ones for IBB in all investigated systems. A linear relation between the Soret coefficients of two components is derived for each system and allows validating experimentally the coefficients
- <sup>25</sup> measured in other experiments.
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# 28 I. INTRODUCTION

29 The study of thermodiffusion in multicomponent systems raises a great level of interest in the scientific community. Molec-30 31 ular diffusion and thermodiffusion play an important role in many 32 natural<sup>1,2</sup> and industrial<sup>3</sup> processes and for the fundamental under-33 standing of the behavior of liquid mixtures.<sup>4-6</sup> Thermodiffusion, or 34 the Soret effect,' refers to a species transfer mechanism due to a local 35 temperature gradient. The experimental techniques for the measure-36 ment of Soret coefficients in binary mixtures are well known and 37 were presented in several reviews.<sup>8-11</sup> In recent years, a large amount 38 of experimental work was devoted to the study of the Soret effect in multicomponent systems.<sup>1</sup> 39

In the present paper, we provide the Soret coefficients obtained from the measurements performed in ternary liquid systems aboard the International Space Station (ISS) during the DCMIX1 (Diffusion Coefficient Measurements in mIXtures) experiment. DCMIX1 is part of the DCMIX program that is endorsed by the European Space Agency and includes four experiments, studying several ternary liquid systems. During the DCMIX1 measurement campaign, a series of experimental runs were performed, studying ternary mixtures composed of 1,2,3,4-tetrahydronaphthalene (THN), isobutylbenzene (IBB), and n-dodecane ( $nC_{12}$ ) with different concentrations at 25 °C. The experimental conditions are such that species transport results from the combined effect of thermal gradient and molecular diffusion. In a ternary system, the diffusive flux  $J_i$  of component i

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 $_{53}$  can be written as<sup>13</sup>

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$$J_i = -\rho \sum_{j=1}^2 D_{ij} \nabla w_j - \rho D'_{T,i} \nabla T,$$

where  $\rho$  is the density of the liquid,  $D_{ij}$  are the molecular diffusion coefficients,  $w_i$  and  $D'_{T,i}$  are, respectively, the mass fraction and thermodiffusion coefficient of component *i*, and *T* is the temperature.

Significant data analysis and processing work is required in order to retrieve accurate values for the Soret coefficients. The raw data were simultaneously analyzed by several research teams and compared prior to publication. In the present paper, we detail the experimental setup and procedure, compare the different data processing methodologies, and report and discuss the obtained Soret coefficients.

### 66 II. EXPERIMENTAL

In this section, we discuss several aspects of the experiments.
First, we explain the principle of the experimental technique in
Sec. II A. The choice of the studied systems, the experimental setup,
and the experimental procedures are described in Sec. II B.

### 71 A. DCMIX experiment

72 The principle of the DCMIX experiment was proposed in 73 Ref. 14 for the experimental determination of the diffusion coeffi-74 cients of liquid mixtures. The concentration gradient used to observe 75 molecular diffusion is created through the Soret effect by plac-76 ing the liquid in a nonuniform temperature field. This idea was 77 already used in a number of previous studies, such as the laser beam 78 deflection technique by Kolodner in 1987,15 but here the chem-79 ical composition field is observed by the means of an interfero-80 metric technique. Modern interferometric techniques allow obtain-81 ing a map of the chemical composition in liquid systems with a high spatial and temporal resolution. The Selectable Optical Diag-82 83 nostic Instrument (SODI) allows obtaining in one single experi-84 ment both the Soret and the diffusion coefficients. In this paper, 85 the study is limited to the determination of the Soret coefficients only.

86 The experiment starts with a homogeneous system at constant 87 temperature; at the beginning of the "Soret step" of a run, a temper-88 ature gradient is created in the liquid by placing the bottom and top 89 walls of the liquid volume at two different temperatures. The tem-90 perature gradient is kept constant, and thermodiffusion induces the 91 migration of the components. Once the system has reached a steady 92 state, in a closed cell, with no convection and no chemical reaction, 93 the diffusion fluxes vanish and the composition gradient along the 94 cell is proportional to the temperature gradient. From Eq. (1), this 95 can be written as

$$\nabla w_i = -S'_{T,i} \nabla T, \tag{2}$$

<sup>97</sup> where we introduced the modified Soret coefficients  $S'_{T,i}$ . 99% of <sup>98</sup> the separation is obtained after about five times the characteris-<sup>99</sup> tic diffusion time. In ternary systems, characteristic diffusion time <sup>100</sup>  $\tau = L^2/(\pi^2 D_s)$  can be computed using the cell height *L* and the <sup>101</sup> smaller eigenvalue  $D_s$  of the diffusion matrix. <sup>16</sup> This corresponds <sup>102</sup> to the end of the *Soret step* of the runs in on-board operations.

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The so-obtained concentration differences  $\Delta w_i$  of the components 103 across the cell provide the Soret coefficients by the relation 104

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$$\Delta w_i = -S'_{T,i} \Delta T, \qquad (3) \qquad 105$$

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where the differences  $\Delta$  are from the top wall with respect to the bottom wall of the cell. After the *Soret step*, the temperature gradient is removed; the "*Diffusion step*" then develops and Eq. (1) applies with a vanishing temperature gradient,

$$J_i = -\rho \sum_{j=1}^2 D_{ij} \nabla w_j.$$
 (4) 110

The typical timeline of an experimental run is shown schematically in Fig. 1.

### **B. Experimental**

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The primary objective of the DCMIX1 experiment is to obtain accurate and reliable experimental data about the diffusive properties of multicomponent systems, in a convection free environment. The project originated from the collaboration between several academic research centers with partners from the oil industry during which binary, ternary, and quaternary Soret coefficients were obtained in microgravity conditions in the SCCO experiment.<sup>17-19</sup> Three chemical species were selected to represent three major families of compounds found in crude oils: THN, IBB, and nC12, respectively, for the families of naphthenic, aromatic, and aliphatic compounds. The selected systems involve three components and are away from the dilution limits. Nondiluted ternary systems carry the main aspects of multicomponent systems, and chemo-diffusive couplings specific to multicomponent systems appear as soon as more than two nondiluted components are diffusing. The concentrations of the systems investigated in DCMIX1 are summarized in Table I.



**FIG. 1.** Principle of an interferometric Soret diffusion experiment. Prior to the experiment, during the thermalization phase, the entire cell is kept at constant temperature. During the "Soret step," a temperature gradient is applied to the liquid and the Soret effect induces a gradient of the chemical components in the system. During the "Diffusion step," the temperature gradient is removed and the diffusion coefficients are quantified by observing the relaxation of the liquid induced by molecular diffusion.

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138 **TABLE I.** Concentrations of the systems investigated in the DCMIX1 experiment.

	Cor f	nponent raction (	mass %)	Experimental runs process
Cell	THN	IBB	nC <sub>12</sub>	in this study
0	50		50	NA
1	10	10	80	16, 21
2	10	80	10	2 <sup>E</sup> , 07, 17, 22, 27
3	80	10	10	See Ref. 12
4	45	10	45	4 <sup>E</sup> , 19, 24
5	40	20	40	5 <sup>E</sup> , 15, 20, 25

<sup>150</sup> In Fig. 2, the mixtures investigated in DCMIX1 are shown with <sup>151</sup> red points. Five primary cells, cells 1–5, were filled with ternary mix-<sup>152</sup> tures, and one companion cell, cell 0, was used to study a binary <sup>153</sup> system with equal mass factions of *THN* and  $nC_{12}$ . The composi-<sup>154</sup> tions are such that points are aligned in the ternary concentration <sup>155</sup> diagram, with the aim of investigating mixing rules. <sup>17,20–23</sup>

156 The diffusion and Soret coefficients of the correspond-157 ing binary systems have been measured by several experimen-158 tal techniques in the frame of the Fontainebleau benchmark,<sup>24</sup> 159 and the ternary diffusion coefficients were recently measured on 160 ground.12,1 For each system investigated during the DCMIX1 campaign aboard the ISS, several experimental runs were performed. 161 162 For cell 1, liquid leaked out of the cell during the measurement cam-163 paign. A bubble appeared in the cell, and only two experimental runs were completed. 164

For each cell, two different durations of the runs were used.
In addition to the "standard runs," "extended runs," denoted with
superscript *E* in tables Table I, have been proposed in the event that



FIG. 2. Concentrations of the systems investigated in DCMIX1. The concentrations of the systems investigated under microgravity conditions in DCMIX1 are shown by red dots in a ternary diagram. Systems characterized by aligned points in the diagram were selected for the investigation of mixing rules.

the diffusion coefficients of one investigated system are significantly lower than foreseen.

Each run starts with a thermalization phase during which the temperature of the cell is stabilized to  $25 \,^{\circ}$ C. The top and bottom cell walls are then brought to 20 and  $30 \,^{\circ}$ C, respectively. A stationary temperature gradient quickly establishes in the liquid, and the thermodiffusion process is monitored during a given time. The temperature gradient is then removed, and isothermal diffusion is observed. The duration of the "*Soret step*" was selected so that the Soret separation attains the steady state. The duration of the "*diffusion step*" was chosen to cover several characteristic molecular diffusion times.

For some runs, data are acquired simultaneously for the companion cell and for a primary cell. The measurements in the companion cell are carried out in order to study the possible influence of the residual gravity on the experiments, a topic of interest for microgravity assessment,<sup>28–31,57</sup> and to cross-check with ground based measurements.

The liquid is placed in a parallelepipedic cell, as shown in Fig. 3. The four lateral sides of the cell are transparent, allowing optical probing. The temperatures of the upper and lower metallic walls of the cell are controlled precisely and independently by Peltier modules. During the DCMIX1 measurement campaign, the six systems presented in Table I are arranged in a cell array and studied sequentially.<sup>32</sup> Details regarding the cell design can be found in Ref. 26.

The chemical composition within the binary system of the companion cell is visualized with a standard Mach-Zehnder type interferometer. A movable two-wavelength interferometer, which can be moved to the selected cell, probes the primary cells.<sup>33</sup> The wavelengths of the laser diodes used are  $\lambda_1 = 670$  nm and  $\lambda_2 = 935$  nm.

The components of the experimental setup were assembled inside the US Destiny module where ISS residual gravity is lowest. A set of parameters monitoring the functioning of the experiment are both simultaneously displayed in real time on ground and stored



**FIG. 3**. Schematic of a DCMIX experimental cell. The liquid volume is sealed by O-rings. Two Peltier elements are used to control the temperatures of copper parts. Temperature sensors probe the temperatures of the copper parts.

TABLE II. Data processing sequences used in the present study.

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210	on flash disks. The data were distributed to the science team by the
211	MARS center. <sup>34</sup>

## 212 III. DATA PROCESSING

213 The data obtained from the experiment are a set of digitized interferograms. The data processing methodology implemented to 214 215 obtain the Soret coefficients from the experimental data consists of 216 a sequence of five main steps. As discussed in Ref. 35, for each step, 217 several possibilities can be envisaged; this results in a wide variety of data processing approaches, as shown diagrammatically in Fig. 4. 218 219 During the course of previous benchmarking for DCMIX1,<sup>12</sup> sev-220 eral teams have processed the same set of experimental data by dif-221 ferent processing schemes. The mass transfer coefficients, obtained 222 by different procedures, have revealed large dispersion. To address this problem, in the present study, we investigate 7 data processing 223 schemes, referred to as DP 1-7 in Table II, and we compare in detail 224 225 the transport coefficients obtained.

The different possible implementations of the 5 steps of Fig. 4
 are discussed in the following.

The capital letters A to E refer to the major successive steps of the data processing sequence. The possible implementations of each step are indicated by numbered panels.

### 231 A. Input experimental data

The first step of the data processing scheme is the selection of the experimental data used for the estimation of the transport coefficients. In Table II, data processing schemes 1–4 analyze the data collected during the *Soret phase* of an experimental run, while data processing schemes 5–7 use the data corresponding to the *diffusion phase* of the runs.

DP	Processing sequence	Authors
1	A1 B1 C1 D3 E3+4	AM, VS (ULB)
2	A1 B1 C1 D3 E2+3	AM, VS (ULB)
3	A1 B1 C3 D3 E4	TT, WK (UB)
4	A1 B2 C1 D4 E3+4	OK, IR, TL (RAS)
5	A2 B2 C1 D4 E3+4	OK, IR, TL (RAS)
6	A2 B1 C3 D2 E4	QG, SVV (ULB)
7	A2 B1 C1 D1 E4	QG, SVV (ULB)

In optical probing, the spatial concentration variation in the liquid is evaluated by measuring changes in the refractive index. During the Soret step of the experimental runs, the refractive index n of the ternary system varies with its temperature and with its chemical composition,

$$\Delta n_i = \frac{\partial n_i}{\partial T} \Big|_{w_1, w_2} \Delta T + \frac{\partial n_i}{\partial w_1} \Big|_{w_2, T} \Delta w_1 + \frac{\partial n_i}{\partial w_2} \Big|_{w_1, T} \Delta w_2, \qquad (5)$$

where the symbol  $\Delta$  here denotes the changes of quantities with respect to their equilibrium values. The thermal and molecular diffusivities differ by about two orders of magnitude, and it is easy to separate the two last terms on the right hand side (RHS) of Eq. (5) from the thermal signal contribution. The thermal field is obtained from the early images of the *Soret step* of the runs, while the images recorded later are used to obtain the concentration changes  $\Delta w_1$ and  $\Delta w_2$ . During the diffusion step of the experiments, the liquid is isothermal and the first term on the RHS of Eq. (5) vanishes. The fringe density significantly increases when the temperature gradient



FIG. 4. Simplified diagram of possible schemes for processing interferometric Soret-diffusion experimental data. The top panels A to E indicate the major successive steps.
 The possible implementations of each step are indicated by numbered panels.

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is imposed across the cell, as easily observed from two experimentalimages shown in Fig. 5.

### 268 B. Image processing

By design, the interpretation of interferometric experimental 269 270 data requires the use of a 5 step image processing method. Before 271 the image processing procedure, the images are cropped and rotated 272 to exclude the regions outside the sample volume and to align the 273 plates of the cell horizontally. The first step, the phase calculation, 274 is the determination, directly from the interferograms, of a wrapped 275 phase change  $\Psi$ . In the second step, a reference image is subtracted from every image since the individual phase values are meaningful 276 only when compared to a reference state.  $\Delta \Psi$  is wrapped into the 277 278 interval  $[-\pi, \pi]$ . The third step, phase unwrapping, allows obtaining the phase change  $\Delta \varphi$  of the light of wavelength  $\lambda$  traversing the sam-279 280 ple along the geometrical path *e* that results from a refractive index 281 change  $\Delta n$ ,

$$\Delta \varphi = \frac{2\pi e}{\lambda} \Delta n. \tag{6}$$

Finally, the unwrapped phase is converted into the refractive index using Eq. (6).

### 285 1. Phase calculation

The image acquisition technique used is a phase shifting inter-286 ferometry.<sup>36,37</sup> It consists in acquiring several fringe images that are 287 288 phase shifted by an integer fraction of  $2\pi$  of the object and calcu-289 lating the resulting phase signal with a phase shifting algorithm. In 290 SODI, phase shifts are obtained by stepping the laser diode currents. 291 For DCMIX1, the selected technique is based on the acquisition of a 292 set of five fringe images with a phase shift of  $\pi/2$ . The acquisition of 293 five images is achieved within less than a second, a time where the 294 refractive index field can be considered constant. This assumption is 295 perfectly reasonable since the characteristic time of the experiments 296 is of the order of several hours. In the data processing schemes DP 1 297 and 2 of Table II, phase images were computed using the Hariharan 298 algorithm.<sup>38</sup> In DP3, a modified<sup>39</sup> version of the Hariharan equation 299 was implemented.<sup>40</sup> In DP 4 and 5, the widely known Fourier filter-300 ing method<sup>41,42</sup> was applied. This method allows reconstructing the 301 optical phase from a single interference image. A detailed descrip-302 tion of the method is provided in Refs. 33 and 43. As discussed 303 in Ref. 38, for many DCMIX images, significant phase shift errors 304 were observed, resulting in strong disturbances of the phase signal 305 when standard stepping algorithms are straightforwardly applied. In

DP 6 and 7, to address this problem, the phase signals were recovered with iterative algorithms.<sup>44</sup> All the above-mentioned methods differ substantially in their basic principles; therefore, one can expect some differences between the obtained signals. Note that even within the same methodology, difference in results obtained by different researchers may arise due to the implementation of the algorithms.

### 2. Reference subtraction

Interferometry, by principle, is a differential measuring technique: the measured quantity is the variation of the refractive index field with respect to a reference, commonly referred to as the "reference image." When processing the images acquired during the Soret phase of the runs, the reference image corresponds to the beginning of the Soret phase, right after the establishment of the temperature gradient in the liquid, so that the reference subtraction allows separating the thermal and compositional parts of the experimental signals of Eq. (5). On the other hand, when performing the processing of the images of the *diffusion phase* of the runs, the reference image is acquired at the end of the thermalization phase of the runs, prior to the *Soret phase*.

### 3. Phase unwrapping

Phase unwrapping is a well-known problem in interferometry, and many different algorithms have been proposed to remove the phase ambiguity.<sup>45</sup> In DP1, DP2, and DP3, a modified<sup>40</sup> version of the Itoh algorithm<sup>46</sup> was implemented; in DP 4 and 5, the wrapped phase images are of sufficient quality, the phase exhibit a strict horizontal alignment, and a one-dimensional sequential phase unwrapper was employed;<sup>33</sup> in DP6 and 7, the Costantini<sup>47</sup> algorithm was used.<sup>48</sup>

### 4. Contrast factors

These image processing operations are performed independently for the two sets of images acquired for the two wavelengths of the two-color interferometer and allow obtaining two series of refractive index maps  $\Delta n_i(x, y, t)$ . The concentration fields are then obtained with the following equation:

$$\begin{pmatrix} \Delta w_1 \\ \Delta w_2 \end{pmatrix} = \begin{pmatrix} n_{1,1}|_2 & n_{1,2}|_1 \\ n_{2,1}|_2 & n_{2,2}|_1 \end{pmatrix}^{-1} \begin{pmatrix} \Delta n_1 \\ \Delta n_2 \end{pmatrix},$$
(7) 341

where we introduced the optical contrast factors  $n_{i,j}|_k$ , defined as

$$u_{i,j}\big|_k = \frac{\partial n_i}{\partial w_j}\big|_{T,P,w_{k,k\neq j}}.$$
(8) 343



FIG. 5. Comparison of typical interfer-	344
ence patterns. Left: pattern recorded dur-	345
ing the Soret phase of an experimental	346
run. Right: pattern recorded during the	347
diffusion phase.	348

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TABLE III. Contrast factors for the 5 ternary systems studied in the DCMIX1 experiment at T = 25 °C. Component 1 is *THN*, component 2 is *IBB*, and component 3
 is nC12. Contrast factors are defined in Eq. (8). Those values were computed from Ref. 49.

Cell	$w_1$	$w_2$	<b>W</b> <sub>3</sub>	$n_{1,1} _2$	$n_{1,2} _1$	$n_{2,1} _2$	$n_{2,2} _1$	Κ
1	10	10	80	0.0960	0.0547	0.0926	0.0521	342
2	10	80	10	0.1248	0.0758	0.1198	0.0714	254
3	80	10	10	0.1427	0.0887	0.1374	0.0838	241
4	45	10	45	0.1149	0.0686	0.1107	0.0655	495
5	40	20	40	0.1164	0.0696	0.1120	0.0667	1092

The contrast factors are experimentally measured in ground experiments. The computed values of the Soret coefficients strongly depend on the values of the contrast factors used for the calculations. In the present study, all teams used identical contrast factors, computed using the methodology and the experimental data reported in Ref. 49 and summarized in Table III.

An algorithm for identification of the transport coefficients requires the inversion of the matrix of optical contrast that can be ill conditioned.<sup>49</sup> The conditioning of a matrix is characterized by a condition number K.<sup>35</sup> The smaller the condition number, the lower the error amplification when computing the concentration of the components from the interferograms.

### 372 C. Data fitting

373 Identification of the mass transport coefficients is performed 374 by fitting the analytical solution of Eq. (1) to the experimental data 375 extracted from the processed images. The concentration distribution can be written in different ways. The most widely used ana-376 lytical solutions are the full path solution<sup>26,35,43,51</sup> that includes all 377 378 available data points, both in time and in space; the gradient solu-379 tion,<sup>33,35,52</sup> similar to the optical beam deflection (OBD) approach,<sup>5</sup> 380 which describes the gradient of concentration at midheight of the 381 cell; and the concentration difference solution,<sup>3</sup> which describes 382 the temporal evolution of the difference of concentration between 383 the top and the bottom of the cell. Each of the above provides both 384 Soret and diffusion coefficients, but the amount of data involved in 385 the identification of the mass transport coefficients is essentially dif-386 ferent and the use of the different approaches can lead to slightly 387 different results. Finally, one can simply analyze the concentration 388 gradient at steady state by processing the image obtained at the end 389 of the Soret phase of the run (or alternatively at the beginning of the 390 diffusion phase, as proposed in Ref. 48). This method allows retriev-391 ing the Soret coefficients directly with Eq. (2) and does not require 3927 identifying the diffusion coefficients. As can be seen from Fig. 6, 393 the two phase signals obtained at different wavelengths are clearly separated from each other. 394

395 In general, the mathematical solution of a Soret diffusion exper-396 iment in ternary mixture comprises six unknowns, four diffusion 397 coefficients  $D_{11}$ ,  $D_{12}$ ,  $D_{21}$ , and  $D_{22}$ , and two Soret coefficients  $S'_{T,1}$ 398 and  $S'_{T,2}$ . To obtain reliable fitting results, different strategies were 399 tested in this study. In the first, as done in DP 7, the six unknowns 400 are fitted directly. This technique, however, provides diffusion coef-401 ficients that are very sensitive to noise. Using specific combinations 402 of unknown quantities in the analytical solutions, the problem can



**FIG. 6.** Typical phase signals obtained after image processing of the data of a DCMIX1 experimental run. The two optical signals, corresponding to the two wavelengths of the two-color interferometer,  $\lambda_1 = 670$  nm,  $\lambda_2 = 935$  nm, are of similar shape but different amplitude.

be converted to four parameters<sup>33</sup> (two Soret coefficients and two diffusion eigenvalues,  $\widehat{D}_1$  and  $\widehat{D}_2$ ). The mathematical details of different models are available elsewhere.<sup>35</sup> This methodology was applied in *DP*2 and *DP*3. Moreover, assuming that the two diffusion eigenvalues are equal,

$$\widehat{D}_1 = \widehat{D}_2 = D_{qb},\tag{9}$$

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meaning that ternary diffusion can be modeled as quasibinary diffusion, the problem is then simplified to a three-parameter fit.<sup>26</sup> This methodology was used in DP1 and DP2. In DP3 to DP5, the mathematical modeling requires defining an amplitude matrix M.<sup>27,52</sup> The fitting identifies 6 unknowns, the four elements of M and the two diffusion eigenvalues. Alternatively, in the steady state concentration gradients method, used in DP6, only the two Soret coefficients are fitted.<sup>48</sup>

We want to emphasize that for the present work, the shapes of the transients and, hence, the diffusion eigenvalues, were not analyzed in full detail since they are irrelevant for the asymptotic amplitudes that determine the Soret coefficients. This becomes most apparent in the quasibinary approximation of Eq. (9), where the two eigenvalues are even set equal. The diffusion eigenvalues of the systems were measured elsewhere, by the Taylor Dispersion Technique (TDT),<sup>16</sup> by the Optical Beam Deflection (OBD),<sup>52</sup> and by the Sliding Symmetric Tubes (SST).<sup>55</sup> Additional experimental data obtained by the SST<sup>56</sup> and by the open ended capillary method<sup>48</sup> were also reported for cell 3 in the frame of a benchmark.<sup>12</sup> Those data are summarized in Table IV.

### **D.** Corrections

Due to the DCMIX cell design, the temperature field in the liquid is not perfectly linear. As a consequence, see Eq. (1), the concentration distribution, and therefore the measured refractive index fields, is also not linear. However, the working equations describing the problem apply linear concentration profiles. As a consequence, optical integration of the deformed refractive index fields leads to underestimated values of the Soret separation. Different suggestions for the correction of the data were proposed. In Ref. 32, the authors use a so-called "optical temperature" (see Sec. IV A) in Eq. (3) to

445	Refs. 5	55 and 56, and by the ope	n ended Capillary in Ref. 48.		
446	С	Reference	$\hat{D}_1 \ (10^{-10} \ \mathrm{m}^2 \ \mathrm{s}^{-1})$	$\hat{D}_2 (10^{-10} \text{ m}^2 \text{ s}^{-1})$	$\bar{D} (10^{-10} \mathrm{m^2} \mathrm{s^{-1}})$
447		TDT16	11.0	0.0	10.25
446	1	IDI OPD <sup>52</sup>	11.9	8.8	10.35
449	1	SST <sup>55</sup>	11	9	6.02 10
450		TDT <sup>16</sup>	10.9	9	9.95
451	2	OBD <sup>52</sup>			9.82
		SST <sup>55</sup>	12	9	10.5
452		Benchmark <sup>12</sup>	6.61	5.48	6.04
453		TDT <sup>16</sup>	7.4	5.3	6.35
454	3	OBD <sup>52</sup>			9.29
455		OEC <sup>48</sup>	6.60	5.50	6.05
456		SST <sup>65</sup>	8.08	5.43	6.75
457		TDT <sup>16</sup>	8.5	6.2	7.35
458	4	OBD <sup>52</sup>			6.65
		SST <sup>55</sup>	7	7	7
459		TDT <sup>16</sup>	8.9	6.5	7.7
460	5	OBD <sup>52</sup>			7.03
		SST <sup>55</sup>	7	4	5.5
461					

**TABLE IV** Diffusion eigenvalues and mean eigenvalue  $\tilde{D}$  for the DCMIX1 systems. Those values were obtained by the Taylor

462 compute the Soret coefficients. In the present study, all the Soret 463 coefficients were computed with a temperature difference of 10 °C, 464 as measured by the temperature sensors. In Refs. 26, 35, 57, and 58, the authors recommend performing a tomography reconstruction of 465 466 the concentration profiles in the center of the cell to account for the 467 curvature of the temperature field. This approach is used in DP2 in 468 our study.

4695 At short times, both in the Soret and the diffusion phase of the 470 runs, the hypothesis of the temporal separation of the thermal and 471 compositional transients is not strictly valid.<sup>20</sup> During the temper-472 ature transient, diffusive concentration changes do happen close to 473 the top and bottom walls of the cell,<sup>59</sup> but are not observed in the 474 interferograms, due to the reference image subtraction. In DP1, DP2, 475 DP4, and DP5, this effect is taken into account by introducing an 476 additional fitting variable, an initial time  $t_0$ , as discussed in Refs. 26, 477 33, and 43.

478 The temperature field in the cell is more linear in the central 479 part, and more curved in the external regions of the cell, approach-480 ing the upper and lower heating elements or the Quartz walls. DP 4, 481 DP5, DP6, and DP7 only take into account a limited central region 482 of the field of view of the interferograms.

### 483 **IV. RESULTS AND DISCUSSION**

### A. Thermal analysis 484

485 The thermal regulation timeline of the cells includes several 486 steps. We present in the following figures the typical evolution of

the temperatures  $T_1$  and  $T_2$  in the top and bottom part of each experimental cell. For all the runs for cells 0-4, the performance of the temperature regulation was very similar. A typical plot of the temperatures  $T_1$  and  $T_2$  for those runs is showed in Fig. 7.

In Fig. 7, the speed of the regulation during the buildup and the removal of the temperature gradient are illustrated by temporal zooms. For all the runs, 90% of the temperature gradient is established or removed within a little less than 1 min and more than 99% is stabilized within 2 min. The third zoom shows that the temperature regulation is stable and precise: during the Soret step, the maximum deviation between the measured and set point temperatures is 0.02 °C; during the diffusion step, it is 0.05 °C. Similar temperature profiles were observed for all runs for cells 0-4. For all runs on cell 5 however, notable deviations from the nominal temperatures were observed throughout the experiments, as depicted in Fig. 8. The cause of the occasional malfunction of the temperature regulation for this cell could not be revealed.

For those runs, numerous temperature spikes were detected, during which the difference between the set-point and measured temperatures was of the order of 0.2–0.4 °C.

As mentioned earlier, the characteristic heat and mass diffu-508 509 sion times differ by about two orders of magnitude. The analysis of the interferometric data at the beginning of the Soret step allows 510 obtaining information about the temperature field across the cell. 511 We report here the data obtained for the binary system, referred 512 513 to as cell 0 in Table I. Both temperatures were stabilized at 25 °C before acquiring a reference image. T<sub>1</sub> was then raised to 30.00 °C, 514

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while  $T_2$  was cooled down to 20.00 °C. 2 min later, a second interferometric image was acquired. This corresponds to more than 517 5 times the characteristic heat diffusion time for the investigated

<sup>518</sup> liquids. The corresponding phase images were calculated and pro <sup>519</sup> cessed as described in Fig. 9. The observed phase change is shown in Fig. 10.

<sup>520</sup> A map of the refractive index change was calculated with <sup>521</sup> Eq. (10). Interferometry measures the average refractive index change across the liquid sample (here, average means integrated along the optical axis of the interferometer). It is then possible to determine a 2D map of the average temperature in the liquid, the "optical temperature"  $T_{opt}$ , 534

$$T_{opt} = \frac{\Delta n_1}{n_{1,T}},$$
 (10) 535



FIG. 8. Typical temperature cycle performed in a DCMIX1 run for cell 5. These measurements show that temperature control did not function nominally for cell 5. Notable deviations from the nominal temperatures were observed. The cause of the malfunction could not be revealed.

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FIG. 9. Image processing steps for the translation of interferometric experimental of a Soret diffusion experiment. Step 1 is phase calculation, step 2 is reference image subtraction, step 3 is phase unwrapping, and step 4 is computation of refractive from the unwrapped phase.

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FIG. 10. Temperature field in cell 0. Top left: phase map recorded right after the establishment of a stationary temperature field in the cell. Top right: colormap of the computed temperature in the liquid. Bottom left: vertical temperature profiles in the liquid. Bottom right: horizontal temperature profiles in the liquid.

where  $n_{1,T} = \partial n_1 / \partial T |_{w_{1,w_2}} = -0.004 47$  is the thermal contrast factor at wavelength  $\lambda_1$ .<sup>60</sup> In Fig. 10, we observe a strong curvature of the temperature field approaching the edges of the cell. The temperature difference between the top and the bottom of the cell is close to 10 °C in the center of the cell but significantly smaller at the Quartz walls. The temperature profiles along several vertical and horizontal lines are plotted in Fig. 10.

### 545 B. Soret coefficients

The refractive index difference between the top and the bottom of the cell  $(n_{tb})_i$  for both wavelengths and the corresponding Soret coefficients obtained by using the 7 different data processing schemes are reported in Table V. We do not report data for cell 3 in the present paper, as it was previously studied in detail.<sup>12,26,32,33,48,54</sup>

551 In Table V, outlier data points corresponding to  $S'_{T,1}$  or  $S'_{T,2}$ 552 and deviating of more than 2 standard deviations from the mean coefficients are indicated by a \* superscript. Based on this set of 553 554 results, we report in Table VI the mean Soret coefficients obtained 555 in the present study, together with the coefficients found in the 556 literature, including coefficients obtained by OBD,<sup>52</sup> by a previ-5578 ous analysis of DCMIX1 data<sup>32,54</sup> and by combination of SST and 558 thermogravitational column experiments (SST + TC).<sup>5</sup>

For cells 1–4, at least 2 Soret coefficients were obtained with a reasonable accuracy. For cell 5, the experimental data did not allow identifying accurately the Soret coefficients. We provide the coefficients obtained for cell 5, but we acknowledge that given the amplitude of the standard deviation, these values should be taken with caution. The first observation is that, in all systems, the heavier component, tetralin, showed a positive Soret effect, which means 565 that it concentrated at the cold side of the cell. Moreover, the magni-566 tude of the separation of tetralin is larger than that of the two other 567 components (except in cell 5). The systems studied through the first 568 three cells are located close to the three corners of the ternary con-569 centration diagram (see Table I), where one of the components is 570 more concentrated than the other two  $(nC_{12} \text{ in cell } 1, IBB \text{ in cell})$ 571 572 2, and THN in cell 3). The comparison of the results obtained for these cells provides an illustration of the complexity of thermodiffu-573 sion in multicomponent mixtures. We do not observe any obvious 574 correlation between the concentration of the components and the 575 576 amplitude of the Soret coefficients. In the present study, we obtained a negative coefficient for IBB, but this observation is not confirmed 577 by previous experimental studies. In cell 2,  $S'_{T,2}$  is larger than  $S'_{T,3}$ , 578 while in cells 1 and 3,  $S'_{T,3}$  is larger. The separation of tetralin is 579 580 significantly larger in cells 4 and 5 than in cells 1-3.

### 1. Comparison of data processing approaches

As indicated in Eq. (2), the steady state thermodiffusive concentration fields are proportional to the temperature field in the cells. Due to the curvature of the temperature field, the refractive index differences measured by interferometry tend to underestimate the Soret separation. Data processing sequences DP1 and DP2 used identical image processing algorithms and mathematical models, the only difference being the tomographic reconstruction of the refractive index fields. Thus, the refractive index differences, and the Soret coefficients, computed by DP2 are significantly larger than the ones obtained by DP1.

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**TABLE V**. Refractive index differences at both wavelengths and Soret coefficients obtained with the 7 data processing sequences of Table II. Components 1, 2, and 3 are, respectively, *THN*, *IBB*, and  $nC_{12}$ ; C is the cell number; DP is the data processing scheme according to Table II; and run is the run reference according to Table I. \* superscript denotes outlier data points.

 $10^{-4}$ 

 $-(n_{tb})_1$ 

6.103

6.086

6.852

6.836

6.107

6.119

5.78

5.77

6.22

 $-(n_{tb})_2$ 

5.929

5.921

6.662

6.645

5.952

5.946

5.73

5.69

6.07

 $S_{T'_1}$ 

9.41

10.07

11.04

10.85

11.0

9.5

\*18.8

\*15.8

12.2

 $10^{-4} \, \mathrm{K}^{-1}$ 

 $S_T'_2$ 

-5.35

-6.53

-6.76

-6.54

-8.1

-5.5

\*-2.24

\*-17.1

-10.0

TABLE V.	(Continued.)
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			$-(n_{tb})_1$	$-(n_{tb})_2$	$S_T'_1$	$S_T'_2$
С	DP	Run	10	-4	$10^{-4}$	$K^{-1}$
		2	5.286	5.092	5.09	-1.41
	-	7	5.251	5.063	5.31	-1.82
	/	12	5.172	5.067	9.00	-8
		22	5.241	5.067	5.91	-2.82
4		4	21.022	20.431	34.9	-27.8
	3	19	20.898	20.312	34.8	-27.8
		24	20.845	20.248	33.4	-25.6
		4	20.719	20.063	27.39	-15.68
	6	19	19.9621	19.3060	24.0	-11.0
		24	19.5198	18.9097	26.6	-16.1
		4	20.8220	20.2560	36.79	-31.28
	7	19	20.6856	20.0665	30.90	-21.60
		24	20.9056	20.3094	34.17	-26.76
5		15	18.65	18.10	47.31	-52.29
	1	20	19.29	18.73	50.84	-57.27
	-	5	19.13	18.71	79.49	-105.4
		25	18.80	18.25	48.64	-54.30
		15	20.96	20.34	55.32	-62.39
	2	20	22.16	21.52	57.41	-64.18
	2	5	20.89	20.54	110.44	-54.22
	7	25	21.23	20.69	70.55	-87.46
		5	19.815	19.193	42.2	-42.1
	3	15	19.105	18.488	37.1	-34.5
	5	20	19.021	19.169	*200.0	*-308
		25	19.442	18.728	19.2	-4.2
		5	*18.27	*17.11	*6.69	*-1.15
	6	10	19.561	18.915	34.7	-29.9
		15	17.46	17.01	57.9	-71.7
		5	18.65	17.93	11.3	7.9
		10	18.5	17.78	8.9	11.7
	7	15	18.3	17.59	11.0	7.9
		20	18.21	17.49	9.0	11.1
		25	18.48	17.82	23.0	-11.9

DP5 results in the most scattered Soret coefficients. In DP5, the optical phases of the experimental data were collected during the *diffusion step* of the experiments. Due to the alignment of the interferometer in wide fringe configuration, the images collected during this step of the runs only contain a few fringes, and the Fourier algorithm results in noisy phase signals.

DP3 and DP7 are based on very different mathematical modeling of the diffusive processes but implement similar image processing algorithms. The coefficients obtained through these two data processing sequences are very consistent. This seems to indicate that the influence of the image processing algorithms is more critical than the mathematical modeling of the experiments.

	5	21	6.26	5.98	*1.0	*9.7
		11	6.161	5.924	4.61	3.17
	6	16	5.790	5.630	9.33	-5.79
		21	5.710	5.520	6.64	-1.21
	7	16	6.314	6.065	4.2	4.17
	/	21	6.181	5.947	4.9	2.7
2		17	5.133	4.978	6.55	-4.01
		02	5.199	5.041	6.58	-3.98
	1	22	5.148	5.004	7.11	-4.91
		27	5.172	5.023	6.93	-4.60
		07r	5.202	5.042	6.50	-3.83
		17	5.714	5.545	7.45	-4.73
		02	5.757	5.578	7.09	-4.09
	2	22	5.730	5.564	7.63	-5.00
		27	5.742	5.578	7.76	-5.20
		07r	5.780	5.622	8.14	-5.78
		2	5.2428	5.087	6.8	-4.3
	3	17	5.2307	5.063	6.2	-3.3
	5	22	5.2122	5.062	7.0	-4.6
		27	5.2272	5.073	6.9	-4.4
		2	5.04	4.87	5.9	-3.0
		17	4.92	4.84	9.3	-8.9
	4	22	4.97	4.82	6.3	-3.8
		27	4.96	4.84	7.6	-5.9
		27 r	4.93	4.85	*9.8	*-9.6
		2	5.06	4.81	*2.1	*3.3
		17	-5.01	-4.79	*2.7	*2.2
	5	22	-4.99	-4.81	4.8	-1.3
		27	-4.99	-4.78	3.4	0.9
		27r	4.98	4.86	7.8	-6.3
		2	5.613	5.416	6.0	-2.4
	6	12	5.359	5.192	6.08	-3.0
		17	5.359	5.192	6.59	-3.78

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694		are, respectively, min, ibb, and no 12. Superscript denotes confected data.						
695	С	References	$S_{T}'_{1}/10^{-4} (K^{-1})$	$S_{T}'_{2}/10^{-4} (K^{-1})$	$S_{T}'_{3}/10^{-4} (K^{-1})$			
696 697		This study	$8.6 \pm 2.8$	$-3.8 \pm 4.8$	$-4.8 \pm 2$			
698		$TC + SST^{55}$	$5.4 \pm 0.7$	3.2				
699	1	OBD <sup>52</sup>	5.8	3.9	-9.0			
700		DCMIX1 <sup>54</sup>	$6.02 \pm 0.4$	$-0.42 \pm 0.2$				
701								
702		This study	$6.7 \pm 1.2$	$-4.1 \pm 2.0$	$-2.6 \pm 0.8$			
703		DCMIX1 <sup>32</sup>	$-7.42(+7.42^{**})$	$-0.59 (-5.90^{**})$				
704	2	$TC + SST^{55}$	$3.1 \pm 0.6$	2.9				
705		OBD <sup>52</sup>	4.1	0.2	-4.4			
706		DCMIX1 <sup>54</sup>	$4.53\pm0.6$	$-0.98\pm0.2$				
707	3	Benchmark <sup>12</sup>	$12.8 \pm 0.4$	$-5.8 \pm 0.3$	-7			
708								
709		This study	$31.40 \pm 4.5$	$-22.6 \pm 7$	$-8.8\pm2.5$			
710	4	$TC + SST^{55}$	$19 \pm 2$	1.0				
711	4	OBD <sup>52</sup>	21.7	-1.4	-20.3			
712		DCMIX1 <sup>54</sup>	$21.5\pm0.6$	$-4.94 \pm 0.4$				
713		This study	44.56 ± 27	$-44.8 \pm 44$	$1.34 \pm 17$			
714	5	$TC + SST^{55}$	$15 \pm 4$	6				
715		OBD <sup>52</sup>	19.5	-1.7	-17.7			
716								

**TABLE VI.** Average Soret coefficients obtained in this study, compared with literature data.<sup>32,52,54,55</sup> Components 1, 2, and 3 are, respectively, *THN*, *IBB*, and *nC*<sub>12</sub>. \*\* superscript denotes corrected data.

In DP7, the mathematical modeling of the diffusive processes
 is simplified and can only be used if the Soret separation actually
 attains steady state at the end of the Soret phase of the runs.

### 720 2. Analysis of errors on the Soret coefficients

<sup>721</sup> In Fig. 11, we have plotted in a  $S'_{T1}$ - $S'_{T2}$  space the Soret coefficients obtained through the 7 data processing sequences together <sup>723</sup> with the coefficients found in the literature.

724 A first observation is that, as discussed in Ref. 29, the coeffi-725 cients obtained with different data processing methods are aligned in 726 the  $S'_{T1}$ - $S'_{T2}$  space. The error of the Soret coefficients has a remarkable property: instead of forming a radially uniform scattering cloud 727 around the solution point  $\{S'_{T1}, S'_{T2}\}$ , it forms a very elongated ellip-728 729 soid, practically degenerated into a line. This means that all data 730 processing sequences of Table II lead to consistent optical analy-731 sis of the experimental data. The dispersion on the obtained Soret 732 coefficients is due to the conversion of optical quantities to concen-733 tration quantities. This step, in Eq. (7), requires inverting the matrix 734 of optical contrast factors. This matrix is quite ill-conditioned, and 735 the inversion amplifies a low optical noise into a large uncertainty in 736 the concentrations. The orientation of the line in the  $S'_{T1}$ - $S'_{T2}$  space 737 is defined by the properties of the contrast factor matrix. In Ref. 61, it 738 has been shown that the directions of the major and the minor axis 739 of the uncertainty ellipsoid are given by the right-singular vectors 740 of the contrast factor matrix. Based on this observation, it appears 741 that DCMIX1 experimental data do not allow retrieving the ternary 742 Soret coefficients with the same accuracy as for typical binary mix-743 tures. However, these data provide a linear correlation between the Soret coefficients. By writing this correlation as

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$$S'_{T,2} = AS'_{T,1} + B,$$
 (11) 745

we obtain the values of parameters A and B provided in Table VII.

This linear correlation corresponds essentially to the result of a single-color experiment. The second detection color narrows the solution space down from a straight line to a line segment, whose length depends on the condition number of the contrast factor matrix.

The consistency of the obtained results shows that, in general, all data processing sequences of Fig. 4 and Table II can reliably be used for the interpretation of ternary thermodiffusion experiments and we cannot point out clear criteria for preferring one data processing methodology over the others. On the other hand, such criteria may appear from a particularity of the raw data itself. The choice of a particular data processing methodology must be made on a case by case basis, depending on the characteristics of the experimental data.

### 3. Comparison with literature data

The comparison of our results with literature data, <sup>32,52,54,55</sup> as 761 summarized in Fig. 11, shows that the coefficients found in previous 762 763 publications are also located on the lines defined by Eq. (11). The 764 coefficients of Refs. 32 and 54 were obtained from previous analysis of DCMIX1 data and computed using similar contrast factor matri-765 ces. These coefficients therefore unsurprisingly display the same 766 trend as our results. Although, in the previous analysis, the authors 767 did not notice and describe the scattering of  $S'_{T,1}$  and  $S'_{T,2}$  because 768

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**FIG. 11.** Comparison of Soret coefficients with literature data, for DCMIX1 cells 1, 2, 4, and 5. The coefficients were obtained through data processing sequences DP1 to DP7 and compared with literature data, including coefficients obtained by the Optical Beam Deflection (OBD) technique,<sup>52</sup> by a previous analysis of DCMIX1 data,<sup>32,54</sup> and by combination of sliding symmetric tubes and thermogravitational column experiments (SST + TG).<sup>55</sup> All the obtained coefficients are aligned in the S' T1-S' T2 space.

**TABLE VII.** Coefficients of the linear correlation between the Soret coefficients obtained in this study.

Cell	А	В
1	-1.6877	0.0011
2	-1.5856	0.0007
4	-1.5449	0.0026
5	-1.6347	26.2379

the conversion of refractive index into concentration in their algorithm was applied at an early stage, which resulted in overlooking the effect.

### V. CONCLUSIONS

The Soret coefficients of a series of five ternary systems were performed under microgravity conditions aboard the International Space Station in the frame of the DCMIX1 experiment. In the present paper, we have detailed the experimental setup, the procedure, and the experimental data analysis. We have provided an extended review of the different possible data processing schemes used in the interpretation of digital interferometric ternary thermodiffusion experiments. We have shown that different choices of image processing algorithm and mathematical modeling of the experiments are possible and lead to consistent results. We have observed that the measured Soret coefficients are aligned in the  $S'_{T,1}$ - $S'_{T,2}$ space and that there remains an indetermination on the values of the measured Soret coefficients due to the ill-conditioned matrix of optical contrast factors. We have derived a linear correlation between the Soret coefficients for each ternary system. These correlations allow for an experimental validation of the Soret coefficients measured by OBD<sup>52</sup> and by the combination SST +  $TG^{55}$  in ground conditions by comparison with the results of the microgravity DCMIX1 experiment.

From the comparison with literature data, we can conclude the consistency of the data obtained from the SODI instrument by different data processing approaches. Besides, we have compared our results with coefficients obtained in ground laboratories, by SST + TC in Ref. 55 or by OBD in Ref. 52. Those coefficients were computed using density and refractive index or refractive index at two different wavelengths (405 and 635 nm), respectively, for the concentration measurements. These techniques are therefore based on different contrast factor matrices, which provide some advantages for this particular system.

Nevertheless, all the coefficients, although measured with very different experimental techniques, using a variety of data processing approaches, and computed with different sets of contrast factors, are all located on the lines of Fig. 11. This observation suggests that the results of DCMIX1 allow for an experimental validation of the coefficients measured under gravity conditions in Refs. 52 and 55. As a general result, the Soret coefficients can be fixed in the direction of the short axis of the confidence ellipsoid with a high accuracy. How far they can be narrowed down in the perpendicular direction of the long axis very strongly depends on the contrast factor matrix and, hence, on the particular ternary mixture and the

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employed experimental technique. For a mixture containing both 830 831 aromatic and aliphatic compounds, it is advantageous to choose 832 one wavelength in the blue, close to the UV-absorption of the delo-833 calized  $\pi$ -electrons.<sup>62</sup> The DCMIX1 system belongs to this class of mixtures. But this advantage may be gone for systems without an 834 835 aromatic compound. Also, the combination of density and refrac-836 tive index detection, as employed in the thermogravitational column 837 technique, can in certain cases profit from superior contrast factor 838 matrices. Unfortunately, no perfect experimental technique exists 839 that could cover all possible mixtures, and a change of the detection 840 wavelengths is not feasible for the microgravity experiments.

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