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Amplification of Light by Molecules with Selectively Oriented States in the Pulsed Electric Field

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The possibility of inversionless amplification of light by dichroic molecules that can be oriented selectively over states by application of an pulsed electric field is analyzed. The numerical simulation of the orientation process of molecules in the external field is considered. As shown the conditions of inversionless amplification with considering of transition between energetic levels may be implemented.

Keywords: inversionless light amplification, molecule, exponential fitting.

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Introduction

When analyzing light interaction that is resonant to energy-level transition, the equality of probabilities of induced emitted and absorbed radiation is expected. According to quantum gain of light it requires to create the inversion of population of energy levels. However, the power of induced emitted and absorbed radiation is determined not only by the population of energy levels of particles, but also by the probabilities of induced transitions, as well as the number of energy-degenerate states. Therefore, population inversion is generally a particular case in which the emission power exceeds the absorption power and, hence, amplification of light takes place [1].

The possibility of inversionless amplification of light in a system of dichroic molecules selectively oriented over states in an external field was considered in [2, 3]. These ideas were subsequently developed by the authors in [4, 5] in which on the basis of the coupled system of kinetic Boltzmann equations for the ground and excited states the effect of the relation between τ_2^{eff} and τ_0 on gain α is numerically analyzed. The authors have shown that to achieve the inversionless amplification the value of alignment electric field \vec{E}_0 must be close to or above

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the breakdown threshold of existing environments, where the studied molecules can be placed. However, if the impulse duration of \vec{E}_0 is in 10^{-9} sec , the electric strength of technically pure liquid increases in some times against the constant field [6].

In this paper we present the usage of the pulsed field \vec{E}_0 as orienting. To calculate the amplification factor α the numerical analysis of dipole molecule orientation on the basis of solutions of nonsteady kinetic equation is used.

1. Physical Model

When external field \vec{E}_0 is acting on a molecular medium, the molecules are oriented in the direction corresponding to the minimum of the potential energy of their interaction with this field [7, 8]. The degree of orientation of the medium as a whole is determined by the orientation parameter p_j , presented as the interaction of the molecule with field to the energy kT of thermal motion, which produces a disorienting effect. For axially symmetric molecules placed in a constant electric field \vec{E}_0 , in a state of $j = 1, 2$ and have constant dipole moment in this state $\vec{\mu}_j$, the orientation parameter p_j , takes the form,

$$p_j = \frac{\vec{\mu}_j \vec{E}_0}{kT}. \quad (1)$$

Interaction energy and, hence, the orientation degree of the molecules in the ground and excited states can be different. In this case, the probabilities of induced transitions with absorption and amplification of polarized light, which are determined by the orientation of molecules relative to the electric field direction in the probe wave, can also be different. This makes it possible in principle to create the conditions for amplification of light with a certain polarization in the absence of population inversion by controlling the degree of orientation in the ground and excited states.

The amplificatin factor $\alpha > 0$ (absorption factor $\alpha < 0$) for molecules oriented in external field \vec{E}_0 and in field \vec{E} of plane-polarized probe radiation has the form

$$\alpha = N\sigma_0 \int_{\Omega} [n_2 f_2(\Omega, E_0) - n_1 f_1(\Omega, E_0)] \cos^2 \vartheta d\Omega, \quad (2)$$

here $\sigma_0 \sim d_{21} \cos \vartheta$ is the absorption-emission cross section of a molecule, d_{21} is the electric dipole moment of the transition, ϑ is the angle between the direction of the electric dipole moment of the transition d_{21} and the probe electric field vector \vec{E} , N is the concentration of particles, n_1 and n_2 are the relative populations of the ground and the upper states, produced by an external pump source, $n_1 + n_2 = 1$, $d\Omega = \sin \vartheta d\vartheta d\phi$ is the solid angle element, $f_1(\Omega, E_0)$ и $f_2(\Omega, E_0)$ are the statistical distribution functions for orientations of molecules in the ground and upper states, which are normalized to unity.

Let us suppose that molecules with energy levels W_1 and W_2 are in thermodynamic equilibrium with the pump field ensuring relative populations n_1 and n_2 of the levels, respectively, such that $W_1 < W_2$. In this case, $n_1 > n_2$, population inversion does not take place, and lifetimes τ_1^{eff} and τ_2^{eff} of the ground and upper states are being defined as

$$\frac{1}{\tau_1^{eff}} = w_{12}^{ind}, \quad \frac{1}{\tau_2^{eff}} = w_{21}^{ind} + w_{21}^{sp}, \quad \frac{\tau_2^{eff}}{\tau_1^{eff}} = \frac{n_2}{n_1}, \quad (3)$$

here $w_{12}^{ind} = w_{21}^{ind}$ is the probability of induced transitions and w_{21}^{sp} is the probability of spontaneous transitions.

The coupled nonstationary system of equations for functions $f_1(\Omega, E_0)$ and $f_2(\Omega, E_0)$ with the boundary (5) and initial (6) conditions and the normalization condition (7) combined with relation (2), makes it possible to solve the problem of calculation of the amplification factor formulated above, [8],

$$\begin{cases} \frac{W}{kT} \frac{\partial f_1}{\partial t} - \frac{1}{\sin \vartheta} \frac{\partial}{\partial \vartheta} \left(\sin \vartheta \left(\frac{\partial f_1}{\partial \vartheta} + f_1 \frac{\partial}{\partial \vartheta} \left(\frac{\mu_1 E_0}{kT} \right) \right) \right) = -\frac{W}{kT} w_{12}^{ind} f_1 + \frac{W}{kT} (w_{21}^{ind} + w_{21}^{sp}) f_2, \\ \frac{W}{kT} \frac{\partial f_2}{\partial t} - \frac{1}{\sin \vartheta} \frac{\partial}{\partial \vartheta} \left(\sin \vartheta \left(\frac{\partial f_2}{\partial \vartheta} + f_2 \frac{\partial}{\partial \vartheta} \left(\frac{\mu_2 E_0}{kT} \right) \right) \right) = -\frac{W}{kT} (w_{21}^{ind} + w_{21}^{sp}) f_2 + \frac{W}{kT} w_{12}^{ind} f_1, \end{cases} \quad (4)$$

$$\left. \frac{\partial f_1}{\partial \vartheta} \right|_{\vartheta=0} = \left. \frac{\partial f_2}{\partial \vartheta} \right|_{\vartheta=0} = 0, \quad \left. \frac{\partial f_1}{\partial \vartheta} \right|_{\vartheta=\pi} = \left. \frac{\partial f_2}{\partial \vartheta} \right|_{\vartheta=\pi} = 0, \quad (5)$$

$$f_1(0, \vartheta) = g_1(\vartheta), \quad f_2(0, \vartheta) = g_2(\vartheta), \quad (6)$$

$$2\pi \int_0^\pi (g_1(\vartheta) + g_2(\vartheta)) \sin \vartheta d\vartheta = 1. \quad (7)$$

Here $W = 6kT\tau_0$ is the responsible for the scale model parameter, τ_0 is the time of stabilization of orientational equilibrium. For numerically solving this problem the exponential fitting method is used [9].

2. Computing experiment

Let us consider the two following cases, in which the effect of inversionless amplification can be manifested most strongly [2–5]:

1. Let us suppose that the constant dipole moment $\vec{\mu}_1$ in the ground state is smaller than dipole moment $\vec{\mu}_2$ in the excited state. In this case the effect of inversionless amplification can be manifested in parallel fields \vec{E} and \vec{E}_0 , then $\vartheta = \vartheta_0$ and the amplification factor α , (2), is given by the formula

$$\alpha = \sigma_0 \int_0^{2\pi} \int_0^\pi (n_2 f_2(\vartheta) - n_1 f_1(\vartheta)) \cos^2 \vartheta d\vartheta d\varphi. \quad (8)$$

2. If the opposite condition $|\vec{\mu}_2| < |\vec{\mu}_1|$ is satisfied, then the molecules in the ground state are predominantly oriented along field \vec{E}_0 . Therefore, to suppress absorption, it is expedient to orient field \vec{E}_0 orthogonally to field \vec{E} . The amplification factor α averaged over molecular orientations has the form

$$\alpha = \sigma_0 \int_0^{2\pi} \int_0^\pi (n_2 f_2(\vartheta) - n_1 f_1(\vartheta)) \sin^3 \vartheta d\vartheta \cos^2 \varphi d\varphi. \quad (9)$$

Let us consider the influence of the orientation parameters p_1 and p_2 on gain α . The problem (4)–(7) can be solved numerically by the exponential fitting method under the following physical parameters: $\tau_0/\tau_1^{eff} = 0.01$, $\tau_0/\tau_2^{eff} = 0.0125$, that corresponding to ratio populations of the states $n_2/n_1 = 0.8$. The external electric field pulse duration $1.0 \cdot 10^{-9} \text{ sec}$ assumed to be equal to $E_0 = 2 \text{ MV/sm}$, that two times above the breakdown threshold of existing environments. The time τ_0 of stabilization of orientational equilibrium assumed to be equal to $\tau_0 = 0.25 \cdot 10^{-9} \text{ sec}$.

Fig. 1a and 1b show the calculated dependences of the amplification factor α as a function of the orientation parameters. Curve (1) corresponds to the situation in which the external electric

field $E_0 = 1MV/sm$ and curve (2) corresponds to the situation in which the external electric field pulse $E_0 = 2MV/sm$. The orientation parameters of the assumed field E_0 are the same value as the dipole moments μ_1 and μ_2 , that are used in papers [4, 5, 9].

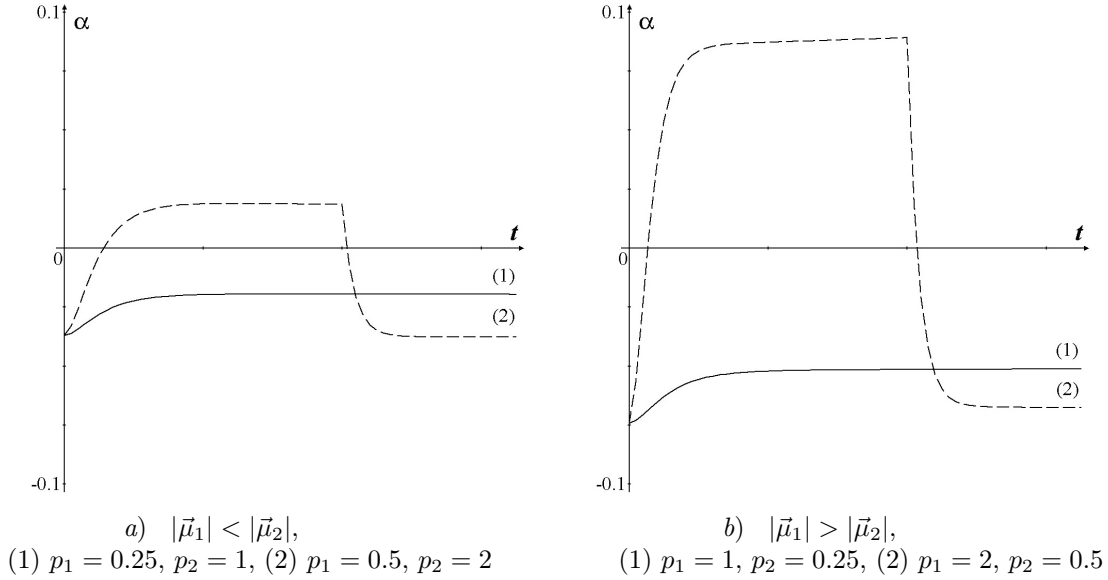


Fig. 1. The influence of the orientation parameters p_1 and p_2 on gain α

Note that, in the first case, $p_2/p_1 = 4$ and external field is a static the parameter α is negative (absorption) and its maximum value is $\alpha_{max} = -0.019$. When the external field is pulse the parameter α is positive (amplification) and its maximum value is $\alpha_{max} = 0.019$. In the second case when $p_1/p_2 = 4$ and external field is a static the parameter α is negative (absorption) and its maximum value is $\alpha_{max} = -0.051$. The positive magnitude of amplification factor α can be reached by switching the external field in the pulsed regime, $\alpha_{max} = 0.089$.

Let us analyze a character of amplification factor modifications. The maximum amplification factor is observed in the case $\mu_1 > \mu_2$, (Fig. 1b). Let us consider a limit situation: $\mu_1 > \mu_2$, $\mu_2 = 0$. In this case, particles in a ground state are oriented lengthwise the \vec{E}_0 field, the orientation of the particles in upper state is isotropic. If the vectors \vec{E} and \vec{E}_0 are orthogonally directed, the influence of the particles in ground state does not decrease the amplification field \vec{E} and the amplification factor α is determined by the first term of (9).

Let us consider the reverse situation: $\mu_2 > \mu_1$, $\mu_1 = 0$. In this case the particles in upper state are oriented lengthwise the \vec{E}_0 field and in their ground state the orientation of the particles is isotropic. The amplification factor α is determined by the gain of the particles in upper state as well as the absorption of particles in ground state, (8).

In general case if μ_1 and μ_2 are different from 0, when meeting the condition $\mu_1 > \mu_2$, the greater degree of orientation is reflected on the particles in ground state, and when the orientation of the vectors of the strengthened field \vec{E} is orthogonal to \vec{E}_0 .

Conclusion

The case study of the investigated sphere is organic molecules, dye molecules in particular. The lifetime in upper state for electric dipole transition of the following molecules is equal to the size of order $10^{-8} - 10^{-9} \text{ sec}$. Orientation time may vary widely depending on the different parameters, that is medium viscosity and the size of molecules, and may also fall within the limits of $10^{-10} - 10^{-12} \text{ sec}$, [7, 8, 10]. The constant dipole moment corresponds to the value of some Debyes. The usage of pulsed orient field produces parameter values of orientation greater than unity in the pre-breakdown field.

Numerical analysis shows that when the parameters of sphere and external field are real, the inversionless gain may be reached on condition of molecule orientation in the pulsed field. The following findings provide the basis for full-scale experiments.

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Усиление света селективно по состояниям ориентированными молекулами в импульсном электрическом поле

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Анализируется возможность безынерсного усиления света дихроичными молекулами, которые могут быть ориентированы селективно по состояниям путем наложения импульсного электрического поля, что позволяет значительно повысить порог пробоя среды. Проведено численное моделирование процесса ориентации молекул во внешнем поле с учетом переходов между энергетическими уровнями и показано, что условия безынерсного усиления могут быть реализованы.

Ключевые слова: безынерсное усиление света, молекула, экспоненциальная подгонка.